## LOYOLA COLLEGE (AUTONOMOUS), CHENNAI - 600034

## B.Sc. DEGREE EXAMINATION - PHYSICS

THIRD SEMESTER - NOVEMBER 2013
MT 3102-MATHEMATICS FOR PHYSICS

Date : 16/11/2013
Dept. No. $\square$ Max. : 100 Marks

## SECTION A

## ANSWER ALL QUESTIONS.

1. Find the $5^{\text {th }}$ derivative of $e^{4 x}$.
2. Find the polar subtangent for the curve $r=e^{\theta c o t \alpha}$.
3. Define symmetric matrix.
4. Write the expansion of $(1-x)^{-p / q}$.
5. Find the laplace transform of cosat.
6. Evalute $L^{-1}\left(\frac{1}{s+a}\right)$.
7. Show that $\cosh 2 x=\cosh ^{2} x+\sinh ^{2} x$.
8. Write down the expansion of $\tan 5 \theta$ in terms of $\tan \theta$.
9. What is the chance that a leap year selected at random will contain 53 Sundays?
10. If two dice are thrown, what is the probability that the sum is greater than 8 ?

## SECTION B

ANSWER ANY FOUR QUESTIONS.
11. Find the angle of intersection between the cardioids $r=a(1+\cos \theta)$ and $r=b(1-\cos \theta)$.
12. Prove that $\frac{1}{2 n+1}+\frac{1}{3} \cdot \frac{1}{(2 n+1)^{3}}+\frac{1}{5} \cdot \frac{1}{(2 n+1)^{5}}+\cdots=\frac{1}{2} \log \left(\frac{n+1}{n}\right)$.
13. Verify Cayley-Hamilton theorem for the matrix $\left(\begin{array}{ccc}1 & 0 & 3 \\ 2 & 1 & -1 \\ 1 & 1 & 1\end{array}\right)$.
14. Find the Laplace transform of $f(t)=\left\{\begin{array}{cc}e^{-t}, & 0<t<4 \\ 0, & t>4\end{array}\right.$.
15. Find $L^{-1}\left(\frac{s}{(s+2)^{2}}\right)$.
16. Express $\sin ^{4} \theta \cos ^{5} \theta$ in a series of cosines of multiples of $\theta$.
17. If $\sin (A+i B)=x+i y$, prove that
(i) $\frac{x^{2}}{\sin ^{2} A}-\frac{y^{2}}{\cos ^{2} A}=1$
(ii) $\frac{x^{2}}{\cosh ^{2} B}+\frac{y^{2}}{\sinh ^{2} B}=1$.
18. Ten coins are thrown simultaneously, find the probability of getting at least 7 heads.

## SECTION C

ANSWER ANY TWO QUESTIONS.

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(2 \times 20=40)
$$

19. (a) Find the maxima and minima of the function $2 x^{3}-3 x^{2}-36 x+10$.
(b) If $y=\sin \left(m \sin ^{-1} x\right)$, then prove that $\left(1-x^{2}\right) y_{n+2}-(2 n+1) x y_{n+1}+\left(m^{2}-n^{2}\right) y_{n}=0$.

$$
(5+15)
$$

20. Find the characteristic roots and associated characteristic vectors of the matrix $\left(\begin{array}{ccc}8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3\end{array}\right)$
21. (a) Find the sum to infinity of the series $1+\frac{1+3}{2!}+\frac{1+3+3^{2}}{3!}+\cdots \infty$.
(b) Solve the equation $\frac{d^{2} y}{d t^{2}}+2 \frac{d y}{d t}+5 y=4 e^{-t}$ given that $y=\frac{d y}{d t}=0$ when $t=0$.

$$
(8+12)
$$

22. (a) Express $\cos 4 \theta$ in terms of $\sin \theta$.
(b) Calculate the mean and standard deviation for the following table giving the age distribution of 542 members:

| Age (in <br> years) | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $\mathbf{8 0 - 9 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of <br> Members | 3 | 61 | 132 | 153 | 140 | 51 | 2 |
|  |  |  |  |  |  |  |  |

